7th Nano and Giga Challenges in Electronics, Photonics and Renewable Energy Tomsk State University (Russia), September 8-22, 2017

Theoretical Study on Energy Conversion Processes of Perovskite Solar Cells

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Computational Materials Science For Energy Conversion



(d)

with e-h



Organic Photovoltaic Cells



Dye-Sensitized Solar Cells



Perovskite Photovoltaics



Interfacial Carrier Transport



Automobile Catalysis



(c)

62 energy (eV)

Photocatalysis

Thermal Transport



Molecular Electronics

Perovskite Photovoltaics

Jin Hyuck Heo^{1†}, Sang Hyuk Im^{1,2†}, Jun Hong Noh^{1†}, Tarak N. Mandal¹, Choong-Sun Lim¹, Jeong Ah Chang¹, Yong Hui Lee¹, Hi-jung Kim¹, Arpita Sarkar¹, Md. K. Nazeeruddin³, Michael Grätzel^{3*} and Sang II Seok^{1,4*} Nature Photonics 5 May 2013





Michael M. Lee,¹ Joël Teuscher,¹ Tsutomu Miyasaka,² Takurou N. Murakami,^{2,3} Henry J. Snaith¹*

SCIENCE 5 November 2012

MAPbl₃ perovskite compounds as a light harvester (Miyasaka *et al.,* JACS 2009)



Key Properties:

- Ambipolar Charge
 Transfer
- Long Charge Carrier
 Lifetime and
 Diffusion Length

Xing et al., Science (2013)



Photocarrier Effective Mass



 $m_e^* = 0.23 \ m_0, m_h^* = 0.29 m_0$ (with Spin-Orbit coupling) This result clearly reveals the ambipolar nature of the material *MA induces the ambipolar (hole-transport) behavior*

Giorgi, Fujisawa, Segawa, Yamashita, JPCC(2014) 118, 12176

Long-Range Balanced Electronand Hole-Transport Lengths in Organic-Inorganic CH₃NH₃PbI₃

18 OCTOBER 2013 VOL 342 SCIENCE

Guichuan Xing,¹* Nripan Mathews,^{2,3,4}*† Shuangyong Sun,² Swee Sien Lim,¹ Yeng Ming Lam,^{2,5} Michael Grätzel,^{3,6} Subodh Mhaisalkar,^{2,3} Tze Chien Sum¹†

Exceed theoretical Shockley-Queisser limit?

Transient Absorption Measurement

"This 0.4-ps hot-hole cooling is much slower than that in most organic semiconductors (~100 fs)"



Carrier Relaxation Lifetime

$$\begin{aligned} \tau_{n\mathbf{k}}^{-1} &= 2\mathrm{Im}\Sigma_{n\mathbf{k}}^{\mathrm{Fan}}(\varepsilon_{n\mathbf{k}}, T = 0\mathrm{K}) \\ &\approx - \begin{bmatrix} \frac{2}{N_{\mathbf{q}}}\sum_{\mathbf{q}\lambda}\sum_{n'\in\mathrm{CB}} \left|g_{nn'\mathbf{k}}^{\mathbf{q}\lambda}\right|^{2} \delta(\varepsilon_{n\mathbf{k}} - \varepsilon_{n'\mathbf{k}-\mathbf{q}} - \omega_{\mathbf{q}\lambda}) & \overset{\mathrm{Phonon\ emission}}{n \in \mathrm{CB}} \\ &\frac{2}{N_{\mathbf{q}}}\sum_{\mathbf{q}\lambda}\sum_{n'\in\mathrm{VB}} \left|g_{nn'\mathbf{k}}^{\mathbf{q}\lambda}\right|^{2} \delta(\varepsilon_{n\mathbf{k}} - \varepsilon_{n'\mathbf{k}-\mathbf{q}} + \omega_{\mathbf{q}\lambda}) & \overset{\mathrm{Phonon\ absorption}}{n \in \mathrm{VB}} \\ & & & \\ &\frac{N_{\mathbf{q}}:\mathrm{Number\ of\ q-points}}{g_{nn'\mathbf{k}}^{\mathbf{q}\lambda}:\mathrm{e-ph\ coupling}} & & & \\ &\omega_{\mathbf{q}\lambda}:\mathrm{Phonon\ frequency} & & & \\ && &$$

$$gF_{n\boldsymbol{k}}^{2}(\omega)\big|_{\mathrm{Fan}} = \frac{1}{N_{q}} \sum_{n' \mathbf{q}\lambda} \frac{\left|g_{nn'\boldsymbol{k}}^{\mathbf{q}\lambda}\right|^{2}}{\varepsilon_{n\boldsymbol{k}}^{KS} - \varepsilon_{n'\boldsymbol{k}-\boldsymbol{q}}^{KS}} \left[2N_{\mathbf{q}\lambda}(T) + 1\right] \delta(\omega - \omega_{\mathbf{q}\lambda}).$$

Lifetime and DOS



Electron-Phonon Coupling



Hot-Hole Cooling



A reduction of the relaxation paths in the small valence DOS as being the origin of the slow hot-hole cooling.

Photophysical Processes and Loss Mechanism



Free-carrier model Yamada et al. JACS (2014) PL and TA measurements *E*_b~25-37meV Miyata et al. Nat. Phys. (2015) Very high magnetic field $E_{\rm b}$ ~16meV (low temp) reduced effective mass 0.104m Phase transition at 160 K orthorhombic \rightarrow tetragonal at 330 K ($k_{\rm B}T^{25}$ meV) tetragonal \rightarrow cubic

Long charge carrier lifetime and diffusion length Combination of

- high charge carrier mobilities
- low charge carrier recombination rates

MAPbl₃ is characterized by

- Strong absorption constant
- High photoluminescence quantum yield



Frost and Walsh, Acc. Chem. Res., 49, 528 (2016)

Hutter et al, Nat. Mater., **16**, 115 (2017)

MAPbl₃ Clusters





1s cluster MA₅₄Pb₂₇I₁₀₈ (567 atoms) Cubic-like, MAI-terminated organic/inorganic cation ratio = 2.00





2i cluster MA₈₄Pb₄₅I₁₇₄ (891 atoms) Tetragonal-like, MAI-terminated organic/inorganic cation ratio = 1.87







MA₉₃Pb₆₀I₂₁₃ (1017 atoms) [001] facet: PbI₂-termonated [100], [010]; MAI-terminated organic/inorganic cation ratio = 1.55

Trajectory of 1s cluster



(a) Side and (b) top view of the VBM(2.05ps).(c) and (d) same for the CBM.

Both VBM and the CBM are spread along the surface edge.



(a) Side and (b) top view of the VBM(2.85ps). (c) and (d) same for the CBM.

VBM is mainly localized into a single Pbl₆ octahedron at the surface. CBM is more spread along one of the …Pb –I–Pb… edges in the z direction.

We can expect that an efficient electron (CBM)-hole (VBM) separation takes place, proving a reduced tendency of recombination once the cluster is excited.

G. Giorgi, K. Yamashita, J. Phys. Chem. Lett., 7, 888-899 (2016)

Trajectory of 2i cluster

G. Giorgi, K. Yamashita, J. Phys. Chem. Lett., 7, 888-899 (2016)



- (a) Lateral and (b) top view of the VBM after 2.65 ps (2.10 eV)
- (c) and (d) for the CBM.
- (e) Lateral and (f) top view for the VBM after 0.90 ps (1.46 eV)
- (g) and (h) for the CBM

Trajectory of 31 cluster



G. Giorgi, K. Yamashita, *J. Phys. Chem. Lett.*, **7**, 888-899 (2016)

(a) Lateral and (b) top view of VBM (after 1.90 ps, 1.73 eV);(c) and (d) the same views for CBM

Rotational Timescale

Rotational autocorrelation function $c(\Delta t)$:

$$c(\Delta t) = \frac{1}{N_{\text{cations}}} \sum_{i} \langle \mathbf{s}_{i}(t) \cdot \mathbf{s}_{i}(t + \Delta t) \rangle$$

where i and si(t) are the index of organic cations and unit vector aligned with the orientation of i-th organic cation, respectively.



H. Uratani, K. Yamashita, submitted (2017)

Charge Separation

Overlap integral q:

$$q = \int_{V_{\text{cell}}} |\psi_{\text{VBM}}(\mathbf{r})| |\psi_{\text{CBM}}(\mathbf{r})| d\mathbf{r} = \int_{V_{\text{cell}}} \sqrt{\rho_{\text{VBM}}(\mathbf{r})\rho_{\text{CBM}}(\mathbf{r})} d\mathbf{r}$$



H. Uratani, K. Yamashita, submitted (2017)

Summary

High performance of lead halide perovskite-based photovoltaic devices

Remarkable carrier properties

- Long carrier diffusion length
- long carrier lifetime
- low electron-hole recombination rate

First-principles molecular dynamics simulations the charge separation is induced by the structural fluctuation of the inorganic lattice

> the charge separation is attributed to the electrostatic potential fluctuation coupled to the inorganic lattice dynamics

the organic cations are unlikely to be essential for carrier properties.



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Cs₅₄Pb₂₇I₁₀₈ cluster



Top view of (a) VBM and (b) CBM (Gray, Pb; purple, I; red, Cs)

The localization of the wave function is more spread out and symmetrically distributed over the whole cluster as a consequence of the replacement of the A-site cation.

The comparison with inorganic halide perovskites supports the idea that the dipole and the rotation of the organic cation play a primary role in the localization of the wave function in MAPbl₃ clusters.



The charge localization causes electron-hole separation and reduces carrier recombination rates.

G. Giorgi, K. Yamashita, J. Phys. Chem. Lett., 7, 888-899 (2016) 21

Summary

- A) The effective masses of photogenerated electrons and holes were estimated to be $m_e^* = 0.23m_0$ and $m_h^* = 0.29m_0$, respectively, including spin–orbit coupling effects. This result is consistent with the long-range ambipolar transport property and with the larger diffusion constant for carriers.
- B) A newly developed MBPT method is applied to analyze the carrier relaxation lifetime of MAPbl₃ perovskites.
- C) Halide Perovskites other than CH₃NH₃Pbl₃ are suggested featuring
 (1) zero dipole moment Guanidium cations,
 (2) aliovalent ionic pairs replace Pb cations.
- D) We have introduced and discussed the properties of zero dimensional (clusters) of organic–inorganic halide perovskites. The present study represents the first analysis focused on the electronic and structural properties of OIHP clusters.
- E) The dipole and the rotation of the organic cation play a primary role in the localization of the wave function in MAPbl₃ clusters. The charge localization causes electron-hole separation and reduces carrier recombination rates.

Review articles: G. Giorgi, K. Yamashita, *J. Mater. Chem. A*, **3**, 8981-8991 (2015) G. Giorgi, K. Yamashita, *Nanotechnology*, in press (2015)

ab initio Molecular Dynamics



G. Giorgi, K. Yamashita, J. Phys. Chem. Lett., 7, 888-899 (2016)

DOS evolution of 1s cluster



The coherent/random orientation of the MA cations thus seems to play a role on the wave function localization preferential sites at the surface.

G. Giorgi, K. Yamashita, J. Phys. Chem. Lett., 7, 888-899(2016)²⁴

Hot-Hole Cooling



A reduction of the relaxation paths in the small valence DOS as being the origin of the slow hot-hole cooling.

■ The 480-nm peak can be assigned to transitions from the VB states along the R-M path.

Dual nature of excited states

Stamplecoskie, Manser, Kamat, Energy Environ. Sci. 8, 208(2015)

Excited state behavior of Pbl_xⁿ⁻ complex in solution



Absorption spectra of 250 μ M PbI₂ solution in dimethylformamide (a) with increasing concentration of MAI from 6mM(b) to 24mM(e)





MA₄Pbl₆, MA₇Pb₂l₁₁ Clusters



G. Giorgi, T. Yoshihara, K. Yamashita, PCCP, 18, 21092 (2016)

Relationship between EDM and FMO



G. Giorgi, T. Yoshihara, K. Yamashita, *PCCP*, **18**, 21092 (2016)

Poster Presentation

4669 Charge Carrier Trapping atSurface Defects of Perovskite SolarCell Absorbers: A First-Principles Study

Hiroki Uratani, Koichi Yamashita J. Phys. Chem. Lett. January 27 (2017) ACS Editor's Choice Selection



Mr. Hiroki Uratani



Nanostructured OIHPs



Nanowires, nanorods, nanoplates Long carrier lifetime Fu, Jin et al. J. Am. Chem. Soc. 2015



Nanocrystals Bandgap tunability

Protesescu, Kovalenko et al. *Nano Lett.* 2015



Colloidal Nanoplates Sharp excitonic absorption

Tyagi, Arveson, Tisdale *J. Phys. Chem. Lett.* 2015



Nanowire Enhanced excitonic nature Im, Grätzel, Park et al. Nano Lett. 2015



Nanocrystals Long photoluminescence times Zhu, Petrich, Smith, Vela et al. ACS Nano 2015

Ion Migration in Organometal Trihalide Perovskite and Its Impact on Photovoltaic Efficiency and Stability

Yongbo Yuan and Jinsong Huang, Acc. Chem. Res., 49, 528 (2016)



Long Electron-Hole Diffusion Lengths



- Absorber (Kim *et al.* 2012, Heo *et al.* 2013) TiO₂/MAPbI₃/HTM
- Electron transporter (Lee *et al.* 2012) Al₂O₃/MAPbl₃/HTM
- Hole transporter (Etgar *et al.* 2012) without HTM





Huang et al. JPCL (2015)

Superior point defect properties

W. J. Yin, T. Shi and Y. Yan, Appl. Phys. Lett., 2014, 104, 063903.



Vacancies (V_{MA} , V_{Pb} , V_{I}), interstitials (MA_{i} , Pb_{i} , I_{i}), cation substitutions (MA_{Pb} , Pb_{MA}) and antisite substitutions (MA_{I} , Pb_{I} , I_{MA} , I_{Pb})



Electrically benign structural disorder

W.-J. Yin, J-H. Yang, J. Kang, Y. Yan, S.-H. Wei, J. Mater. Chem. A, 2014.



(a–i) are (partial) DOS of pristine CsPbI₃ and polycrystalline CsPbI₃ with Σ 3(111) and Σ 5(310) GBs. (j) and (k) are atomic structures at Σ 3(111) and Σ 5(310) GBs respectively.

Halide Perovskites other than $CH_3NH_3PbI_3(1)$



H.J. Snaith et al, J. Phys. Chem. Lett. (2014) 5, 1511



A large hysteresis in the current-voltage curves may be attributed to the motion of organic cations with a permanent dipole moment in response to the applied electric field.



Organic cations that have a zero dipole moment and a molecular size qwell fitted to the lead iodine cavity.

Giorgi, Fujisawa, Segawa, Yamashita, J. Phys. Chem. C, 119, 4694 (2015).

Halide Perovskites other than $CH_3NH_3PbI_3$ (2)











Effective mass of carriers (A- Γ direction) FAPbl₃ m_h *=0.302 m_0 , m_e *=0.403 m_0 GAPbl₃ m_h *=0.385 m_0 , m_e *=0.359 m_0

Ratio: m_h^*/m_e^*

 $FAPbI_{3}$ (0.75), $GAPbI_{3}$ (1.07) GAPbI₃ has a more marked ambipolar behaviour than $FAPbI_{3}$



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Guanidinium: A Route to Enhanced Carrier Lifetime and Open-Circuit Voltage in Hybrid Perovskite Solar Cells

Nicholas De Marco,^{†,‡} Huanping Zhou,^{†,‡} Qi Chen,^{†,‡} Pengyu Sun,[†] Zonghao Liu,^{†,‡} Lei Meng,[†] En-Ping Yao,[†] Yongsheng Liu,^{†,‡} Andy Schiffer,[‡] and Yang Yang^{*,†,‡}



We speculate that guanidinium ions serve to suppress formation of iodide vacancies and passivate under-coordinated iodine species at grain boundaries and within the bulk through their hydrogen bonding capability.

These results present a simple method for suppressing nonradiative carrier loss in hybrid perovskites to further improve performances toward highly efficient solar cells.

Band Structures





Comparison with Pbl₃⁻



Only CsPbl₃ has long lifetime region of holes.

Long lifetime comes from the small DOS.

Generalized Eliashberg Function

Phonon modes contributing to the carrier relaxation



Holes are decayed through the motions of Pb and I, not Cs.

Difference of A-site cation does not alter the decay mechanism. H. Kawai, G.Giorgi, A. Marini, K. Yamashita, *Nano Lett.*, *15*, *3103-3108* (2015)

Optical Excitations



Bulk t-MAPbl₃



(a) PAO/PBE band structure, (b) DOS/PDOS (E_g =1.57 eV at Γ) (c) Lateral and top view of VBM, (d) CBM

Photon recycling in lead iodide perovskite solar cells Science 351 1430 (2016)

Luis M. Pazos-Outón,¹ Monika Szumilo,¹ Robin Lamboll,^{1*} Johannes M. Richter,^{1*} Micaela Crespo-Quesada,² Mojtaba Abdi-Jalebi,¹ Harry J. Beeson,¹ Milan Vrućinić,¹ Mejd Alsari,¹ Henry J. Snaith,³ Bruno Ehrler,⁴ Richard H. Friend,¹† Felix Deschler¹†



Together with high radiative recombination yields and long carrier lifetimes, these properties raise the question of whether absorption and reemission of excited carriers can occur during the transport. "Photon recycling" does indeed play a central role, allowing considerable increases over current descriptions in the characteristic lengths for charge and energy transport.

Halide Perovskites other than CH₃NH₃Pbl₃

Pb-free Perovskites

- Replacing Pb with other group IVA elements, Ge, Sn.
- Mixed-(Sn, Pb) perovskites
- Aliovalent ionic pairs replace Pb cations

 $\begin{array}{l} \mathsf{MATI}_{0.5}\mathsf{Bi}_{0.5}\mathsf{I}_3 \ (\mathsf{MTBI}) \\ \mathsf{MAIn}_{0.5}\mathsf{Bi}_{0.5}\mathsf{I}_3 \ (\mathsf{MIBI}) \end{array}$



(e)) lateral and (f) top view of the optimized MTBI cell. Bandstructure without (g) and with (h) SOC effect inclusion for MTBI.

Bandgap with SOC 0.84 eV for MTBI.

Reduced effective mass 0.31 (0.33) Ratio between the two carrier effective masses 0.83 (0.89) for MAPbI₃ (MTBI)



(b) VBM and (d) CBM wavefunctions of MTBI

G. Giorgi, K. Yamashita, Chem. Lett., **44**, 826 (2015). 43

Computational Screening



Giustino et al (JPCL 2016) Woodward et al (CM 2016) Botti et al (JMCC 2016)

 $(MA)_2 KBiCl_6$ Indirect band gap 3.02 eV(calc) 3.04 eV(exp) Cheetham et al (Mater. Horizons 2016)

Band Gaps of the Lead-Free Halide Double Perovskites $Cs_2BiAgCl_6$ and $Cs_2BiAgBr_6$ from Theory and Experiment J. Phys. Chem. Lett. 2016, 7, 2579

Marina R. Filip,[†] Samuel Hillman,[‡] Amir Abbas Haghighirad,[‡] Henry J. Snaith,[‡] and Feliciano Giustino^{*,†}



 $\begin{array}{c} \mbox{Indirect band gap (eV)} \\ \mbox{GW Exp} \\ \mbox{Cs}_2 \mbox{BiAgCl}_6 & 2.2 & 2.4 \\ \mbox{Cs}_2 \mbox{BiAgBr}_6 & 1.8 & 1.9 \end{array}$

Thermal Transport (1)



The rotational motion of methylammonium cations is considered responsible for phonon transport suppression.

T. Hata, G.Giorgi, K. Yamashita, Nano Lett., 16, 2749-2753 (2016)

Thermal Transport (2)



Pb-I (black thin line) MA translational (blue thick line) rotational (orange thick line) mixed motions (green thick line)

Suppression Mechanism:

the rotations are coupled with translational motions of cations, via which inorganic lattice vibrations are coupled and scatter each other.

T. Hata, G.Giorgi, K. Yamashita, *Nano Lett.*, **16**, 2749-2753 (2016)

Nanostructured OIHPs



Nanowires, nanorods, nanoplates Long carrier lifetime Fu, Jin et al. J. Am. Chem. Soc. 2015



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Nanowire Enhanced excitonic nature Im, Grätzel, Park et al. Nano Lett. 2015



Nanocrystals Long photoluminescence times Zhu, Petrich, Smith, Vela et al. ACS Nano 2015

Averages Volume and Bandgap



The calculated average band gap (~1.58 eV) recovers that of the bulk (1.57 eV); an average diameter of 32.7 Å recover the electronic properties of the bulk.

G. Giorgi, K. Yamashita, J. Phys. Chem. Lett., 7, 888-899 (2016) 48

Nanoscale Charge Localization Induced by Random Orientations of Organic Molecules in Hybrid Perovskite CH₃NH₃Pbl₃ Jie Ma and Lin-Wang Wang, *Nano Lett.*, **15**, 248 (2015)



Figure 6. Charge densities of the CBM and VBM states of an equilibrium structure, which is taken from a snapshot of the Monte Carlo simulation at T = 300 K in the 20 736-atom supercell. Both the CBM and VBM are still strongly localized and separated, although the localization sizes increase.